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A new layer compound Nb₄SiC₃ predicted from first-principles theory

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Abstract

We predicted a new layer compound Nb₄SiC₃ using the first-principles method. The structural stability, mechanical, electronic, theoretical hardness and optical properties of Nb₄SiC₃ were investigated. A stable Nb₄SiC₃ phase appears in the α -type crystal structure. Moreover, the predicted Nb₄SiC₃ is a metal and exhibits covalent nature. Nb₄SiC₃ has a theoretical hardness of 10.86 GPa, which is much higher than Nb₄AlC₃; at the same time, it is more ductile than Nb₄AlC₃. The strong covalent bonding in Nb₄SiC₃ is responsible for its high bulk modulus and hardness. Nb₄SiC₃ exhibits slightly anisotropic elasticity. Furthermore, its optical properties are also analysed in detail. It is shown that Nb₄SiC₃ might be a better candidate material as a coating to avoid solar heating than Ti₄AlN₃.

1. Introduction

Layered ternary compounds, $M_{n+1}AX_n$ (where M is an early transition metal, A is an A group element, X is C or N and $n = 1-3$), have received tremendous attention due to their extraordinary mechanical, physical and chemical properties [1]. The layered structure of these compounds results in their unique combination of metallic and ceramic properties, such as high bulk modulus, high melting point, low density, damage tolerance, microscale ductility at room temperature and resistance to thermal shock and high-temperature oxidation [1-4].

Up to now, more than 50 M_2AX compounds, five M_3AX_2 compounds (Ti₃SiC₂, Ti₃GeC₂, Ti₃AlC₂, Ti₃SnC₂ and Ta₃AlC₂) and six M_4AX_3 compounds (Ti₄AlN₃, Ti₄SiC₃, Ti₄GeC₃, Ta₄AlC₃, Nb₄AlC₃ and V₄AlC₃) have been synthesized. Previous studies on M_4AX_3 compounds focused mainly on phase stability, electronic structure, chemical bonding, mechanical and optical properties [5-12]. Recently, Nb₄AlC₃ was synthesized by annealing Nb₂AlC at 1700 °C. Nb₄AlC₃ possessed a low hardness, high fracture toughness and excellent mechanical properties at high temperatures;

at the same time, it may display quasi-ductility [13-15]. Although Nb₄AlC₃ has these excellent properties, there may be other compounds with superior properties that remain to be discovered. For example, Nb₄AlC₃ has a low hardness due to the weakness of Nb-Al bonds, and therefore it is likely that the combination of Nb and other atoms will give a new M_4AX_3 compound with a high hardness.

In this paper, we proposed a new layer compound Nb₄SiC₃ and predicted its properties, such as mechanical, electronic and optical properties. We found that Nb₄SiC₃ has better mechanical and optical properties than Nb₄AlC₃ and Ti₄AlN₃.

2. Computational details

The calculations were performed using the CASTEP code based on density functional theory with the generalized gradient approximation (GGA) in the scheme of Perdew-Burke-Ernzerhof [16]. The ion-electron interaction was modelled by ultrasoft Vanderbilt-type pseudopotentials [17]. The elastic constants were calculated by the 'stress-strain' method. Mulliken charges were calculated according to the formalism described by Segall *et al* [18]. A plane-wave cutoff energy of 450 eV was employed throughout

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the calculation. Geometry optimization was achieved using convergence thresholds of 1×10^{-5} eV atom⁻¹ for total energy, 0.03 eV Å⁻¹ for maximum force and 0.001 Å for displacement. The tolerance in the self-consistent field (SCF) calculation is 1×10^{-6} eV atom⁻¹. For the sampling of the Brillouin zone, the electronic structures and optical properties used $12 \times 12 \times 4$ and $14 \times 14 \times 4$ k -point grids generated according to the Monkhorst–Pack scheme [19], respectively.

The optical properties of Nb₄SiC₃ are investigated by the frequency-dependent dielectric function $\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega)$ which is mainly connected with the electronic structures. The imaginary part $\varepsilon_2(\omega)$ of the dielectric function $\varepsilon(\omega)$ is calculated from the momentum matrix elements between the occupied and the unoccupied electronic states and given by

$$\varepsilon_2(\omega) = \frac{2e^2\pi}{\Omega\varepsilon_0} \sum_{k,v,c} |\langle \psi_k^c | \hat{u} \cdot r | \psi_k^v \rangle|^2 \delta(E_k^c - E_k^v - E),$$

where ω is the light frequency, e is the electronic charge and ψ_k^c and ψ_k^v are the conduction and valence band wave functions at k , respectively. The real part $\varepsilon_1(\omega)$ is derived from the imaginary part $\varepsilon_2(\omega)$ by the Kramers–Kronig transformation. All other optical constants, such as the absorption spectrum, the energy-loss spectrum and reflectivity, are derived from $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ [20].

3. Results and discussions

3.1. Structural and elastic properties

Nb₄AlC₃ has two types of crystal structures [14]: the α -type has an atom arrangement of ABABACBCBC, while the β -type has an atom arrangement of ABABABABAB. The structural parameters of α - and β -type Nb₄AlC₃ are presented in table 1. The structures of α - and β -type Nb₄SiC₃ were constructed by substituting the Al atoms with the Si atoms in the two types of crystal structures of Nb₄AlC₃, respectively. The predicted lattice parameters and atom positions of the different Nb₄SiC₃ phases are also displayed in table 1. Density functional theory

with GGA usually overestimates the lattice parameters and underestimates the bulk moduli [21]. We also calculated the total energies of the different Nb₄SiC₃ phases. The total energy ($-13\,567.32$ eV) of α -Nb₄SiC₃ is lower than that ($-13\,566.41$ eV) of β -Nb₄SiC₃. Therefore, a stable Nb₄SiC₃ phase appears in the α -type crystal structure, which is the same as Nb₄AlC₃. In the following investigation, we focus mainly on the properties of α -Nb₄SiC₃.

In order to study the mechanical properties of α -Nb₄SiC₃, we calculated its elastic constants, bulk modulus B , shear modulus G and Young's moduli E . The results are shown in table 1, together with the theoretical results of α -Nb₄AlC₃ for comparison. The C_{11} of α -Nb₄SiC₃ is 11 GPa smaller than that of α -Nb₄AlC₃, and this leads to the lower resistances against the principal strain ε_{11} . However, the C_{33} of α -Nb₄SiC₃ is 46 GPa larger than that of α -Nb₄AlC₃, and this leads to higher resistances against the principal strain ε_{33} . The C_{44} of α -Nb₄SiC₃ is 34 GPa larger than that of α -Nb₄AlC₃, thereby higher resistances to basal and prismatic shear deformations. The bulk modulus B of α -Nb₄SiC₃ is higher than that of α -Nb₄AlC₃, and this leads to a higher resistance to the volume change. The shear modulus G of α -Nb₄SiC₃ is very close to that of α -Nb₄AlC₃. Therefore, α -Nb₄SiC₃ has the same resistance to the shape change as α -Nb₄AlC₃. In order to evaluate the elastic anisotropy of the material, we also calculated the ratio between linear compressibility coefficients k_c/k_a . For hexagonal crystals, k_c/k_a can be expressed as $k_c/k_a = (C_{11} + C_{12} - 2C_{13})/(C_{33} - C_{13})$. The k_c/k_a value of α -Nb₄SiC₃ is equal to 1.15, and therefore it has a slight anisotropy on elasticity.

On the other hand, the elastic constants of α -Nb₄SiC₃ can satisfy the well-known Born stability criteria [22]:

$$C_{11} > 0, \quad C_{11} - C_{12} > 0, \quad C_{44} > 0, \\ (C_{11} + C_{12})C_{33} - 2C_{13}^2 > 0.$$

It is known that α -Nb₄SiC₃ is mechanically stable under elastic strain perturbations. The ductility of a material can be roughly estimated by the value of shear-modulus-to-bulk-modulus ratios (G/B) [23–27]. A low (high) G/B value

Table 1. Predicted lattice parameters (Å), atomic positions, elastic constants C_{ij} (GPa), bulk modulus B (GPa), shear modulus G (GPa), Young's moduli E (GPa) and shear-modulus-to-bulk-modulus ratio (G/B) of Nb₄SiC₃.

	α -Nb ₄ SiC ₃	β -Nb ₄ SiC ₃	α -Nb ₄ AlC ₃ ^a	β -Nb ₄ AlC ₃ ^a
Space group	$P6_3/mmc$	$P6_3/mmc$	$P6_3/mmc$	$P6_3/mmc$
Lattice constants	$a = 3.1819$ $c = 22.9877$	$a = 3.1326$ $c = 23.6468$	$a = 3.1296$ $c = 24.1208$	$a = 3.1128$ $c = 24.7089$
Atomic position				
Nb1	(1/3, 2/3, 0.0574)	(1/3, 2/3, 0.05655)	(1/3, 2/3, 0.0553)	(1/3, 2/3, 0.05449)
Nb2	(0, 0, 0.16408)	(1/3, 2/3, 0.6646)	(0, 0, 0.1574)	(1/3, 2/3, 0.6581)
Si/Al	(1/3, 2/3, 1/4)	(1/3, 2/3, 1/4)	(1/3, 2/3, 1/4)	(1/3, 2/3, 1/4)
C1	(0, 0, 0)	(0, 0, 0)	(0, 0, 0)	(0, 0, 0)
C2	(2/3, 1/3, 0.113 07)	(0, 0, 0.113 97)	(2/3, 1/3, 0.1086)	(0, 0, 0.109 99)
C_{11}, C_{33}, C_{44}	403, 374, 195		413, 328, 161	
C_{12}, C_{13}	167, 165		124, 135	
G	142		144	
B	241		214	
E	$E_x = 303, E_z = 278$		$E_x = 344, E_z = 260$	
G/B	0.59		0.67	

^a Reference [14].

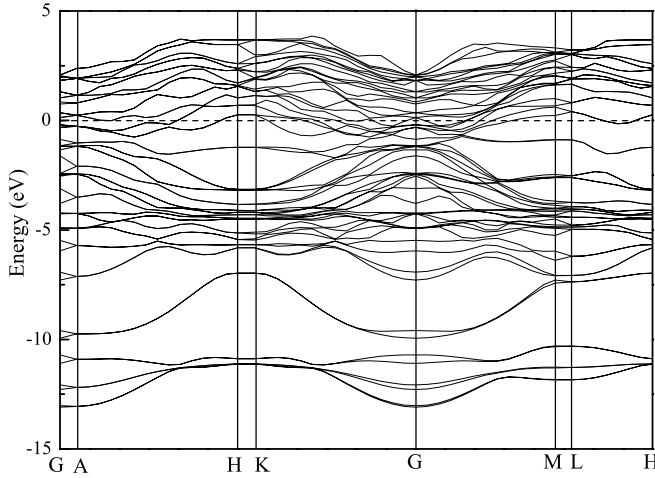


Figure 1. Energy band structure of α -Nb₄SiC₃.

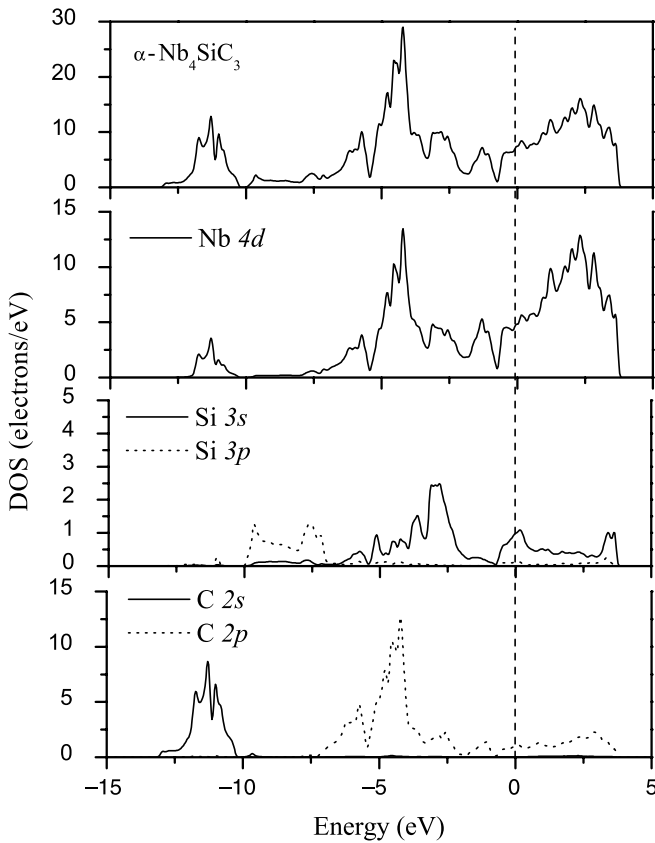


Figure 2. Total and partial DOS of α -Nb₄SiC₃.

shows ductility (brittleness). The G/B value of α -Nb₄SiC₃ is lower than that of α -Nb₄AlC₃. Therefore, α -Nb₄SiC₃ is more ductile than α -Nb₄AlC₃ and exhibits a high shear deformation resistance.

3.2. Electronic properties and theoretical hardness

The energy band structure and densities of states (DOSs) of α -Nb₄SiC₃ are shown in figures 1 and 2, respectively. The energy band structure is calculated along the high-symmetry directions in the Brillouin zone. There are many bands crossing

Table 2. Calculated Mulliken bond overlap population P^μ , bond length d^μ (Å) and Vickers hardness $H_{v\text{calc}}$ (GPa) of α -Nb₄SiC₃.

Bond	d^μ	P^μ	$P^{\mu'}$	v_b^μ	H_v^μ	$H_{v\text{calc}}$
C–Nb	2.179	0.99	0.021	9.882	15.76	10.86
	2.239	1.00	0.021	10.72	13.9	
	2.262	1.00	0.021	11.054	13.21	
Si–Nb	2.697	0.88	0.021	18.736	4.81	

the Fermi level, suggesting that Nb₄SiC₃ is a metal. The lowest energy bands from -13 to -10 eV are dominated by the hybridized Nb 4d and C 2s states. The energy bands between -10 and -7.5 eV consist mainly of Si 3p states, with little contribution from its 3s states. The energy bands between -7.5 and -0.76 eV are dominated by the hybridized Nb 4d/Si 3s and C 2p states. Therefore, Nb₄SiC₃ appears to have covalent nature. Moreover, the peaks of Si 3s are weaker than those of the Nb 4d and C 2p states. The number of peaks was also less than those of Nb and C. Furthermore, the hybridized Nb 4d and C 2s states appear in a lower energy range. These results indicate that the Nb–C bond is stronger than the Nb–Si bond. In addition, the energy bands near and above the Fermi level are attributed to Nb 4d states and antibonding states.

We also performed the Mulliken bond populations in order to understand the bonding behaviour of Nb₄SiC₃ and obtain its theoretical Vickers hardness. The theoretical hardness of crystals with metallic bonding can be calculated as follows [28, 29]:

$$H_v = \left[\prod_{\mu} (H_v^{\mu})^{n^{\mu}} \right]^{1/\sum n^{\mu}}$$

$$H_v^{\mu} \text{ (GPa)} = 740(P^{\mu} - P^{\mu'})(v_b^{\mu})^{-5/3},$$

where P^μ is the Mulliken population of the μ -type bond, $P^{\mu'}$ is the metallic population of the μ -type bond and v_b^μ is the volume of a bond of type μ . The calculated results are shown in table 2. The bond populations indicate the overlap degree of the electron cloud of two bonding atoms. Its highest and lowest values imply that the chemical bond exhibits strong covalency and ionicity, respectively. It can be seen that the C–Nb bonds possessed stronger covalent bonding than the Si–Nb bonds. The results are consistent with our DOS calculation. Moreover, the hardness of Nb₄SiC₃ (10.86 GPa) is higher than Nb₄AlC₃ (2.6 GPa) [15]. The strong covalent bonding in Nb₄SiC₃ is responsible for its high bulk modulus and hardness.

3.3. Optical properties

The calculated results on the dielectric function, the absorption spectrum, conductivity and the energy-loss spectrum are shown in figures 3(a)–(d), respectively. In our calculation, we used a 0.5 eV Gaussian smearing. The imaginary part $\epsilon_2(\omega)$ of the dielectric function is very large below 3 eV, which is due to transitions within the Nb 4d bands, and the $\epsilon_2(\omega)$ spectrum above 3 eV arises from Si/C p \rightarrow Nb d electronic transitions. The large negative value of $\epsilon_1(\omega)$ indicates that the Nb₄SiC₃ crystal has a Drude-like behaviour. The absorption spectrum rises sharply below 8.38 eV and presents three peaks between

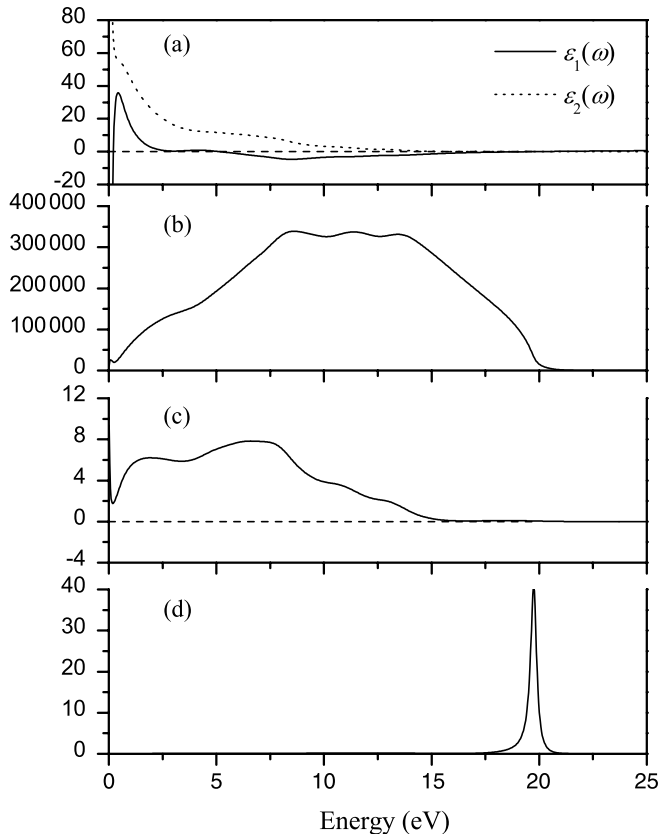


Figure 3. Optical constants of α -Nb₄SiC₃. (a) Imaginary part $\epsilon_2(\omega)$ and real part $\epsilon_1(\omega)$ of the dielectric function $\epsilon(\omega)$, (b) absorption spectrum, (c) photoconductivity and (d) energy-loss spectrum.

9 and 14 eV, and then decreases rapidly in the high-energy region. Three peaks are associated with the transition from Si/C p to Nb d states. Photoconductivity is the increase in the electrical conductivity of a material as a result of absorbing photons [30]. For Nb₄SiC₃, there is photoconductivity when the photon energy is equal to 0 eV. The reason is that Nb₄SiC₃ has no band gap. Therefore, photocurrent can be generated within a wide range of photon energies. The energy-loss spectrum describes the energy loss of a fast electron traversing in the material [31]. Its peak is defined as the bulk plasma frequency ω_p , which occurs where $\epsilon_2 < 1$ and ϵ_1 reaches the zero point [32, 33].

The reflectivity spectra of Nb₄SiC₃, Ti₄AlN₃ [12] and TiN [34] are compared in figure 4. The spectrum of TiN shows a sharp dip from 1.5 to 2.7 eV. Moreover, TiN has a goldlike colour due to high reflectivity for red light and low reflectivity for blue light [35]. Therefore, the reflectance spectrum of TiN is selective. Compared with the reflectance spectrum of TiN, that of Nb₄SiC₃ has no strong edge and colour and does not greatly change at different wavelengths. Therefore, the reflectance spectrum of Nb₄SiC₃ is nonselective and very similar to that of Ti₄AlN₃. According to the nonselective characteristic of the reflectance spectrum of Ti₄AlN₃, Li *et al* [12] concluded that Ti₄AlN₃ could reduce solar heating and enhance the infrared emittance, and therefore the equilibrium temperature of its surface will be moderate in strong sunlight. Based on the conclusion, Nb₄SiC₃ might also be used as

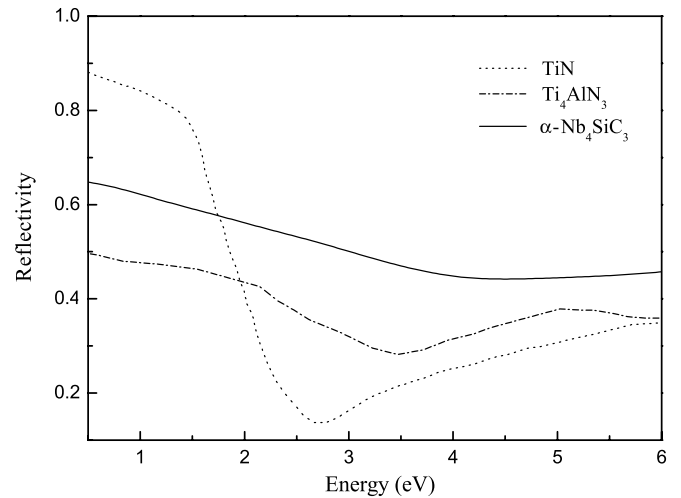


Figure 4. Reflectivity spectra of α -Nb₄SiC₃, Ti₄AlN₃ [12] and TiN [34].

a coating to avoid solar heating. Moreover, Nb₄SiC₃ may well be a better material to avoid solar heating because the reflectance spectrum of Nb₄SiC₃ exhibits less change at different wavelengths than that of Ti₄AlN₃. On the other hand, we also find that the reflectivity of Nb₄SiC₃ is always higher than that of Ti₄AlN₃. Therefore, the capability of Nb₄SiC₃ to reflect solar light is stronger than Ti₄AlN₃.

4. Conclusions

In summary, a new layer compound Nb₄SiC₃ has been predicted using the first-principles method. We investigated its structural stability, mechanical properties, electronic structure, theoretical hardness and optical properties. A stable Nb₄SiC₃ phase appears in the α -type crystal structure. The electronic structures of Nb₄SiC₃ reveal that it is a metal and exhibits covalent nature. Moreover, the C–Nb bonds possessed stronger covalent bonding than the Si–Nb bonds. The strong covalent bonding in Nb₄SiC₃ is responsible for its high bulk modulus and hardness. The elastic constants, bulk modulus, shear modulus and Young's moduli of α -Nb₄SiC₃ are calculated. The results show that Nb₄SiC₃ is more ductile and has a higher hardness than α -Nb₄AlC₃. α -Nb₄SiC₃ also exhibits slight anisotropic elasticity. Finally, the dielectric function, the absorption spectrum, the conductivity, the energy-loss spectrum and reflectivity were obtained and discussed in detail. It is shown that Nb₄SiC₃ might be a better candidate material as a coating to avoid solar heating than Ti₄AlN₃. We hope that the theoretical predictions will inspire experimental investigation on Nb₄SiC₃.

Acknowledgments

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